## CONSTANTS, CONVERSIONS, and CHARACTERS

| DECIMAL MULTIPLIER PREFIXES |  |  |
| :---: | :---: | :---: |
| Prefix | Symbol | Multiplier |
| exa | E | $10^{18}$ |
| peta | P | $10^{15}$ |
| tera | T | $10^{12}$ |
| giga | G | $10^{9}$ |
| mega | M | $10^{6}$ |
| kilo | k | $10^{3}$ |
| hecto | h | $10^{2}$ |
| deka | da | $10^{1}$ |
| deci | d | $10^{-1}$ |
| centi | c | $10^{-2}$ |
| milli | m | $10^{-3}$ |
| micro | $\mu$ | $10^{-6}$ |
| nano | n | $10^{-9}$ |
| pico | p | $10^{-12}$ |
| femto | f | $10^{-15}$ |
| atto | a | $10^{-18}$ |
|  |  |  |


| EQUIVALENCY SYMBOLS |  |
| :---: | :---: |
| Symbol | Meaning |
| $\propto$ | Proportional |
| $\sim$ | Roughly equivalent |
| $\approx$ | Approximately |
| $\cong$ | Nearly equal |
| $=$ | Equal |
| $\equiv$ | Identical to, defined as |
| $\neq$ | Not equal |
| $\gg$ | Much greater than |
| $>$ | Greater than |
| $\geq$ | Greater than or equal to |
| $\ll$ | Much less than |
| $<$ | Less than |
| $\leq$ | Less than or equal to |
| $\vdots$ | Therefore |
| $\vdots$ | Degrees |
| $\prime$ | Minutes or feet |
|  | Seconds or inches |


| UNITS OF LENGTH |  |
| :---: | :---: |
| 1 inch (in) | 2.54 centimeters (cm) |
| 1 foot (ft) | $=30.48 \mathrm{~cm}=0.3048 \mathrm{~m}$ |
| 1 yard (yd) | $\simeq 0.9144$ meter |
| 1 meter (m) | 39.37 inches |
| 1 kilometer (km) | $\simeq 0.54$ nautical mile |
|  | 0.62 statute mile |
|  | 1093.6 yards |
|  | $\approx 3280.8$ feet |
| (sm or stat. mile) | $\simeq 0.87$ nautical mile |
|  | $\simeq 1.61$ kilometers |
|  | = 1760 yards |
|  | $=5280$ feet |
| $\begin{array}{r} 1 \text { nautical mile } \\ \text { (nm or naut. mile) } \end{array}$ | $\simeq 1.15$ statute miles |
|  | 1.852 kilometers |
|  | 2025 yards |
|  | 6076 feet |
| 1 furlong | $=1 / 8 \mathrm{mi}(220 \mathrm{yds})$ |

## UNITS OF SPEED

$$
\begin{aligned}
1 \text { foot } / \mathrm{sec}(\mathrm{fps}) & \cong 0.59 \mathrm{knot}(\mathrm{kt})^{*} \\
& \cong 0.68 \mathrm{stat} \cdot \mathrm{mph} \\
& \cong 1.1 \mathrm{kilometers} / \mathrm{hr} \\
1000 \mathrm{fps} & \cong 600 \mathrm{knots} \\
1 \text { kilometer } / \mathrm{hr} & \cong 0.54 \mathrm{knot} \\
(\mathrm{~km} / \mathrm{hr}) & \cong 0.62 \mathrm{stat} . \mathrm{mph} \\
& \cong 0.91 \mathrm{ft} / \mathrm{sec} \\
& \\
1 \mathrm{mile} / \mathrm{hr}(\mathrm{stat} .) & \cong 0.87 \mathrm{knot} \\
(\mathrm{mph}) & \cong 1.61 \mathrm{kilometers} / \mathrm{hr} \\
& \cong 1.47 \mathrm{ft} / \mathrm{sec} \\
& \cong 1.15 \mathrm{stat} \cdot \mathrm{mph} \\
1 \mathrm{knot} * & \cong 1.69 \mathrm{feet} / \mathrm{sec} \\
& \cong 1.85 \mathrm{kilometer} / \mathrm{hr} \\
& \cong 0.515 \mathrm{~m} / \mathrm{sec}
\end{aligned}
$$

*A knot is 1 nautical mile per hour.

## UNITS OF VOLUME

| 1 gallon | $\cong 3.78$ liters |
| ---: | :--- |
|  | $\cong 231$ cubic inches |
|  | $\cong 0.1335$ cubic ft |
|  | $\cong 4$ quarts |
|  | $\cong 8$ pints |
| 1 fl ounce | $\cong$ |
|  | 29.57 cubic centimeter (cc) |
|  | or milliliters (ml) |
| $1 \mathrm{in}^{3}$ | $\cong 16.387 \mathrm{cc}$ |

UNITS OF AREA

1 sq meter $\cong 10.76 \mathrm{sq} \mathrm{ft}$
1 sq in $\cong 645$ sq millimeters ( mm )
$=1,000,000 \mathrm{sq} \mathrm{mil}$
$1 \mathrm{mil}=0.001$ inch
1 acre $=43,560 \mathrm{sq} \mathrm{ft}$

$$
\begin{aligned}
& \text { UNITS OF WEIGHT } \\
& 1 \text { kilogram }(\mathrm{kg}) \cong 2.2 \text { pounds (lbs) } \\
& 1 \text { pound } \cong 0.45 \mathrm{Kg} \\
&=16 \text { ounce (oz) } \\
& 1 \mathrm{oz}=437.5 \text { grains } \\
& 1 \text { carat } \cong 200 \mathrm{mg} \\
& 1 \text { stone }(\mathrm{U} . \mathrm{K} .) \cong 6.36 \mathrm{~kg}
\end{aligned}
$$

NOTE: These are the U.S. customary (avoirdupois) equivalents, the troy or apothecary system of equivalents, which differ markedly, was used long ago by pharmacists.

## UNITS OF POWER / ENERGY

$$
\begin{aligned}
& 1 \mathrm{H} . \mathrm{P} .=33,000 \mathrm{ft}-\mathrm{lbs} / \mathrm{min} \\
&=550 \mathrm{ft}-\mathrm{lbs} / \mathrm{sec} \\
& \cong 746 \mathrm{Watts} \\
& \cong 2,545 \mathrm{BTU} / \mathrm{hr} \\
&(\mathrm{BTU}=\mathrm{British} \text { Thermal Unit) } \\
& 1 \mathrm{BTU} \cong 1055 \mathrm{Joules} \\
& \cong 778 \mathrm{ft}-\mathrm{lbs} \\
& \cong 0.293 \mathrm{Watt}-\mathrm{hrs}
\end{aligned}
$$

## SCALES <br> OCTAVES

"N" Octaves $=$ Freq to Freq x $2^{N}$
i.e. One octave would be 2 to 4 GHz Two Octaves would be 2 to 8 GHz
Three octaves would be 2 to 16 GHz

## DECADES

"N" Decades $=$ Freq to Freq $\times 10^{\mathrm{N}}$
i.e. One decade would be 1 to 10 MHz

Two decades would be 1 to 100 MHz
Three decades would be 1 to 1000 MHz

TEMPERATURE CONVERSIONS

$$
\begin{gathered}
{ }^{\circ} \mathrm{F}=(9 / 5){ }^{\circ} \mathrm{C}+32 \\
{ }^{\circ} \mathrm{C}=(5 / 9)\left({ }^{\circ} \mathrm{F}-32\right) \\
{ }^{\circ} \mathrm{K}={ }^{\circ} \mathrm{C}+273.16 \\
{ }^{\circ} \mathrm{F}=(9 / 5)\left({ }^{\circ} \mathrm{K}-273\right)+32 \\
{ }^{\circ} \mathrm{C}={ }^{\circ} \mathrm{K}-273.16 \\
{ }^{\circ} \mathrm{K}=(5 / 9)\left({ }^{\circ} \mathrm{F}-32\right)+273
\end{gathered}
$$

## UNITS OF TIME

1 year $=365.2$ days
1 fortnight $=14$ nights ( 2 weeks)
1 century $=100$ years
1 millennium $=1,000$ years
NUMBERS

$$
\begin{aligned}
1 \text { decade }= & 10 \\
1 \text { Score }= & 20 \\
1 \text { Billion }= & 1 \times 10^{9} \text { (U.S.) } \\
& \text { (thousand million) } \\
= & 1 \times 10^{12} \text { (U.K.) }
\end{aligned}
$$

## RULE OF THUMB FOR ESTIMATING DISTANCE TO LIGHTNING / EXPLOSION:

km - Divide 3 into the number of seconds which have elapsed between seeing the flash and hearing the noise.
miles - Multiply 0.2 times the number of seconds which have elapsed between seeing the flash and hearing the noise.
Note: Sound vibrations cause a change of density and pressure within a media, while electromagnetic waves do not. An audio tone won't travel through a vacuum but can travel at $1100 \mathrm{ft} / \mathrm{sec}$ through air. When picked up by a microphone and used to modulate an EM signal, the modulation will travel at the speed of light.

| Physical Constant | Quoted Value | S* | SI unit | Symbol |
| :---: | :---: | :---: | :---: | :---: |
| Avogadro constant | $6.0221367 \times 10^{23}$ | 36 | $\mathrm{mol}^{-1}$ | $\mathrm{N}_{\mathrm{A}}$ |
| Bohr magneton | $9.2740154 \times 10^{-24}$ | 31 | $\mathrm{J} \cdot \mathrm{T}^{-1}$ | $\mu_{\text {B }}$ |
| Boltzmann constant | $1.380658 \times 10^{-23}$ | 12 | $\mathrm{J} \cdot \mathrm{K}^{-1}$ | $\mathrm{k}\left(=\mathrm{R} \mathrm{N}_{\mathrm{A}}\right.$ ) |
| Electron charge | $1.60217733 \times 10^{-19}$ | 49 | C | -e |
| Electron specific charge | $-1.75881962 \times 10^{11}$ | 53 | $\mathrm{C} \cdot \mathrm{kg}^{-1}$ | -e/me |
| Electron rest mass | $9.1093897 \times 10^{-31}$ | 54 | kg | $\mathrm{m}_{\mathrm{e}}$ |
| Faraday constant | $9.6485309 \times 10^{4}$ | 29 | $\mathrm{C} \cdot \mathrm{mol}^{-1}$ | F |
| Gravity (Standard Acceleration) | $\begin{aligned} & 9.80665 \text { or } \\ & 32.174 \end{aligned}$ | 0 | $\begin{aligned} & \mathrm{m} / \mathrm{sec}^{2} \\ & \mathrm{ft} / \mathrm{sec}^{2} \end{aligned}$ | g |
| Josephson frequency to voltage ratio | $4.8359767 \times 10^{14}$ | 0 | $\mathrm{Hz} \cdot \mathrm{V}^{-1}$ | 2e/hg |
| Magnetic flux quantum | $2.06783461 \times 10^{-15}$ | 61 | Wb | $\phi_{\text {o }}$ |
| Molar gas constant | 8.314510 | 70 | $\mathrm{J} \cdot \mathrm{mol}^{-1} \cdot \mathrm{~K}^{-1}$ | R |
| Natural logarithm base | $\cong 2.71828$ | - | dimensionless | $e$ |
| Newtonian gravitational constant | $6.67259 \times 10^{-11}$ | 85 | $\mathrm{m}^{3} \cdot \mathrm{~kg}^{-1} \cdot \mathrm{~s}^{-2}$ | $G$ or K |
| Permeability of vacuum | $4 \pi \times 10^{-7}$ | d | H/m | $\mu_{0}$ |
| Permittivity of vacuum | $\cong 8.8541878 \times 10^{-12}$ | d | F/m | $\epsilon_{\text {o }}$ |
| Pi | $\cong 3.141592654$ |  | dimensionless | $\pi$ |
| Planck constant | $6.62659 \times 10^{-34}$ | 40 | J.s | h |
| Planck constant/2 $\pi$ | $1.05457266 \times 10^{-34}$ | 63 | J.s | $\mathrm{h}(=\mathrm{h} 2 \pi)$ |
| Quantum of circulation | $3.63694807 \times 10^{-4}$ | 33 | $\mathrm{J} \cdot \mathrm{s} \cdot \mathrm{kg}{ }^{-1}$ | $\mathrm{h} / 2 \mathrm{~m}_{\mathrm{e}}$ |
| Radius of earth (Equatorial) | $\begin{aligned} & 6.378 \times 10^{6} \text { or } \\ & 3963 \end{aligned}$ |  | m miles |  |
| Rydberg constant | $1.0973731534 \times 10^{7}$ | 13 | $\mathrm{m}^{-1}$ | $\mathrm{R}_{\chi}$ |
| Speed of light | $2.9979246 \times 10^{8}$ | 1 | $\mathrm{m} \cdot \mathrm{s}^{-1}$ | c |
| Speed of sound <br> (dry air @ std press \& temp) | 331.4 | - | $\mathrm{m} \cdot \mathrm{s}^{-1}$ | - |
| Standard volume of ideal gas | $22.41410 \times 10^{-3}$ | 19 | $\mathrm{m}^{3} \cdot \mathrm{~mol}^{-1}$ | $\mathrm{V}_{\mathrm{m}}$ |
| Stefan-Boltzmann constant | $5.67051 \times 10^{-8}$ | 19 | $\mathrm{W} \cdot \mathrm{K}^{-4} \cdot \mathrm{~m}^{-2}$ | $\sigma$ |

* S is the one-standard-deviation uncertainty in the last units of the value, d is a defined value.
(A standard deviation is the square root of the mean of the sum of the squares of the possible deviations)

| THE SPEED OF LIGHT |  |  |  |
| :---: | :---: | :---: | :---: |
| ACTUAL | UNITS | RULE OF THUMB | UNITS |
| $\cong 2.9979246 \times 10^{8}$ | $\mathrm{~m} / \mathrm{sec}$ | $\approx 3 \times 10^{8}$ | $\mathrm{~m} / \mathrm{sec}$ |
| $\cong 299.79$ | $\mathrm{~m} / \mathrm{\mu sec}$ | $\approx 300$ | $\mathrm{~m} / \mathrm{\mu sec}$ |
| $\cong 3.27857 \times 10^{8}$ | $\mathrm{yd} / \mathrm{sec}$ | $\approx 3.28 \times 10^{8}$ | $\mathrm{yd} / \mathrm{sec}$ |
| $\cong 5.8275 \times 10^{8}$ | $\mathrm{NM} / \mathrm{hr}$ | $\approx 5.8 \times 10^{8}$ | $\mathrm{NM} / \mathrm{hr}$ |
| $\cong 1.61875 \times 10^{5}$ | $\mathrm{NM} / \mathrm{sec}$ | $\approx 1.62 \times 10^{5}$ | $\mathrm{NM} / \mathrm{sec}$ |
| $\cong 9.8357105 \times 10^{8}$ | $\mathrm{ft} / \mathrm{sec}$ | $\approx 1 \times 10^{9}$ | $\mathrm{ft} / \mathrm{sec}$ |

## SPEED OF LIGHT IN VARIOUS MEDIUMS

The speed of EM radiation through a substance such as cables is defined by the following formula:

$$
V=c /\left(\mu_{\mathrm{r}} \epsilon_{\mathrm{r}}\right)^{1 / 2}
$$

Where: $\quad \mu_{\mathrm{r}}=$ relative permeability $\epsilon_{\mathrm{r}}=$ relative permittivity
The real component of $\epsilon_{\mathrm{r}}=$ dielectric constant of medium.

EM propagation speed in a typical cable might be $65-90 \%$ of the speed of light in a vacuum.

## APPROXIMATE SPEED OF SOUND (MACH 1)

| Sea Level (CAS/TAS) |  | $\mathbf{3 6 , 0 0 0} \mathrm{ft}^{*}(\mathrm{TAS})$ | (CAS) |
| :---: | :---: | :---: | :---: |
| $1230 \mathrm{~km} / \mathrm{hr}$ | Decreases | $1062 \mathrm{~km} / \mathrm{hr}$ | $630 \mathrm{~km} / \mathrm{hr}$ |
| 765 mph | Linearly | 660 mph | 391 mph |
| 665 kts | To $\Rightarrow$ | 573 kts | 340 kts |

* The speed remains constant until $82,000 \mathrm{ft}$, when it increases linearly to $1215 \mathrm{~km} / \mathrm{hr}(755 \mathrm{mph}, 656 \mathrm{kts})$ at $154,000 \mathrm{ft}$. Also see section 8-2 for discussion of Calibrated Air Speed (CAS) and True Airspeed (TAS) and a plot of the speed of sound vs altitude.

| SPEED OF SOUND |  |
| :---: | :---: |
| IN VARIOUS MEDIUMS |  |
| Substance | Speed (ft/sec) |
| Vacuum | Zero |
| Air | 1,100 |
| Fresh Water | 4,700 |
| Salt Water | 4,900 |
| Glass | 14,800 |

DECIMAL / BINARY / HEX CONVERSION TABLE

| Decimal | Binary | Hex | Decimal | Binary | Hex | Decimal | Binary | Hex |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 00001 | 01 h | 11 | 01011 | 0 Bh | 21 | 10101 | 15 h |
| 2 | 00010 | 02 h | 12 | 01100 | 0 Ch | 22 | 10110 | 16 h |
| 3 | 00011 | 03 h | 13 | 01101 | 0 Dh | 23 | 10111 | 17 h |
| 4 | 00100 | 04 h | 14 | 01110 | 0 Eh | 24 | 11000 | 18 h |
| 5 | 00101 | 05 h | 15 | 01111 | 0 Fh | 25 | 11001 | 19 h |
| 6 | 00110 | 06 h | 16 | 10000 | 10 h | 26 | 11010 | 1 Ah |
| 7 | 00111 | 07 h | 17 | 10001 | 11 h | 27 | 11011 | 1 Bh |
| 8 | 01000 | 08 h | 18 | 10010 | 12 h | 28 | 11100 | 1 Ch |
| 9 | 01001 | 09 h | 19 | 10011 | 13 h | 29 | 11101 | 1 Dh |
| 10 | 01010 | 0 Ah | 20 | 10100 | 14 h | 30 | 11110 | 1 Eh |

When using hex numbers it is always a good idea to use " $h$ " as a suffix to avoid confusion with decimal numbers.
To convert a decimal number above 16 to hex, divide the number by 16 , then record the integer resultant and the remainder. Convert the remainder to hex and write this down - this will become the far right digit of the final hex number. Divide the integer you obtained by 16 , and again record the new integer result and new remainder. Convert the remainder to hex and write it just to the left of the first decoded number. Keep repeating this process until dividing results in only a remainder. This will become the left-most character in the hex number. i.e. to convert 60 (decimal) to hex we have $60 / 16=3$ with 12 remainder. 12 is C (hex) - this becomes the right most character. Then $3 / 16=0$ with 3 remainder. 3 is 3 (hex). This becomes the next (and final) character to the left in the hex number, so the answer is 3 C .

GREEK ALPHABET

| Case |  | Greek Alphabet Name | English Equivalent | Case |  | Greek <br> Alphabet <br> Name | English Equivalent |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Upper | Lower |  |  | Upper | Lower |  |  |
| A | $\alpha$ | alpha | a | N | $v$ | nu | n |
| B | $\beta$ | beta | b | $\Xi$ | $\xi$ | xi | X |
| $\Gamma$ | $\gamma$ | gamma | g | O | 0 | omicron | ŏ |
| $\Delta$ | $\delta$ | delta | d | $\Pi$ | $\pi$ | pi | p |
| E | $\epsilon$ | epsilon | ě | P | $\rho$ | rho | r |
| Z | $\zeta$ | zeta | Z | $\Sigma$ | $\sigma$ | sigma | S |
| H | $\eta$ | eta | $\overline{\text { è }}$ | T | $\tau$ | tau | t |
| $\Theta$ | $\theta$, v | theta | th | $\Upsilon$ | $v$ | upsilon | u |
| I | 1 | iota | i | $\Phi$ | $\phi, \varphi$ | phi | ph |
| K | к | kappa | k | X | $\chi$ | chi | ch |
| $\Lambda$ | $\lambda$ | lambda | 1 | $\Psi$ | $\psi$ | psi | ps |
| M | $\mu$ | mu | m | $\Omega$ | $\omega$ | omega | ō |

## LETTERS FROM THE GREEK ALPHABET COMMONLY USED AS SYMBOLS

| Symbol | Name | Use |
| :---: | :---: | :---: |
| $\alpha$ | alpha | space loss, angular acceleration, or absorptance |
| $\beta$ | beta | 3 dB bandwidth or angular field of view [radians] |
| $\Gamma$ | Gamma | reflection coefficient |
| $\gamma$ | gamma | electric conductivity, surface tension, missile velocity vector angle, or gamma ray |
| $\Delta$ | Delta | small change or difference |
| $\delta$ | delta | delay, control forces and moments applied to missile, or phase angle |
| $\epsilon$ | epsilon | emissivity [dielectric constant] or permittivity [farads/meter] |
| $\eta$ | eta | efficiency or antenna aperture efficiency |
| $\Theta$ | Theta | angle of lead or lag between current and voltage |
| $\theta$ or $\cup$ | theta | azimuth angle, bank angle, or angular displacement |
| $\Lambda$ | Lambda | acoustic wavelength or rate of energy loss from a thermocouple |
| $\lambda$ | lambda | wavelength or Poisson Load Factor |
| $\mu$ | mu | micro $10^{-6}$ [micron], permeability [henrys/meter], or extinction coefficient [optical region] |
| $\nu$ | nu | frequency |
| $\pi$ | pi | 3.141592654+ |
| $\rho$ | rho | charge/mass density, resistivity [ohm-meter], VSWR, or reflectance |
| $\Sigma$ | Sigma | algebraic sum |
| $\sigma$ | sigma | radar cross section [RCS], Conductivity [1/ohm-meter], or Stefan-Boltzmann constant |
| T | Tau | VSWR reflection coefficient |
| $\tau$ | tau | pulse width, atmospheric transmission, or torque |
| $\Phi$ | Phi | magnetic/electrical flux, radiant power [optical region], or Wavelet's smooth function [low pass filter] |
| $\phi$ or $\varphi$ | phi | phase angle, angle of bank, or beam divergence [optical region] |
| $\Psi$ | Psi | time-dependent wave function or Wavelet's detail function [high pass filter] |
| $\psi$ | psi | time-independent wave function, phase change, or flux linkage [weber] |
| $\Omega$ | Omega | Ohms [resistance] or solid angle [optical region]. Note: inverted symbol is conductance [mhos] |
| $\omega$ | omega | carrier frequency in radians per second |

MORSE CODE and PHONETIC ALPHABET

| A - alpha | -- | J - juliett | --- | S - sierra | -•• | 1 | ----- |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B - bravo | - ••• | K - kilo | -•- | T - tango | - | 2 | -•-- |
| C - charlie | -•-• | L - lima | --•• | U - uniform | -•- | 3 | -••-- |
| D - delta | -•• | M - mike | -- | V - victor | -••- | 4 | -•••- |
| E-echo | $\bullet$ | N - november | - | W - whiskey | -- | 5 | -•••• |
| F - foxtrot | -•-• | O - oscar | -- - | X - x-ray | -•• | 6 | -•••• |
| G - golf | - | P - papa | ---• | Y - yankee | -•-- | 7 | --••• |
| H - hotel | $\cdots \cdot \bullet$ | Q - quebec | --•- | Z - zulu | --•• | 8 | ---•• |
| I - india | -• | R - romeo | --• | 0 | ----- | 9 | ----• |

Note: The International Maritime Organization agreed to officially stop Morse code use by February 1999, however use may continue by ground based amateur radio operators (The U.S. Coast Guard discontinued its use in 1995).

## Basic Math / Geometry Review

## EXPONENTS

$$
\begin{gathered}
a^{x} a^{y}=a^{x+y} \\
a^{x} / a^{y}=a^{x-y} \\
\left(a^{x}\right)^{y}=a^{x y} \\
a^{0}=1
\end{gathered}
$$

Example:

$$
\frac{x}{\sqrt{x}}=x \cdot x^{-\frac{1}{2}}=x^{\left(1-\frac{1}{2}\right)}=x^{\frac{1}{2}}=\sqrt{x}
$$

## LOGARITHMS

$\log (x y)=\log x+\log y$
$\log (x / y)=\log x-\log y$
$\log \left(x^{N}\right)=N \log x$
If $z=\log x$ then $x=10^{z}$
Examples: $\log 1=0$
$\log 1.26=0.1 ; \quad \log 10=1$
if $10 \log \mathrm{~N}=\mathrm{dB} \#$,
then $10^{(\mathrm{dB} \# / 10)}=\mathrm{N}$

## TRIGONOMETRIC FUNCTIONS

$$
\sin x=\cos \left(x-90^{\circ}\right)
$$

$$
\cos x=-\sin \left(x-90^{\circ}\right)
$$

$\tan \mathrm{x}=\sin \mathrm{x} / \cos \mathrm{x}=1 / \cot \mathrm{x}$
$\sin ^{2} \mathrm{x}+\cos ^{2} \mathrm{x}=1$

A radian is the angular measurement of an arc which has an arc length equal to the radius of the given circle, therefore there are $2 \pi$ radians in a circle. One radian $=360^{\circ} / 2 \pi=57.296 \ldots .{ }^{\circ}$


## TRIANGLES

Angles: $A+B+C=180^{\circ}$
$c^{2}=a^{2}+b^{2}-2 a b \cos C$
Area $=1 / 2 b h=1 / 2 a c \sin B$
$c=\sqrt{d^{2}+h^{2}}$


## SPHERE



## DERIVATIVES

Assume: $\mathrm{a}=$ fixed real $\# ; \mathrm{u}, \mathrm{v} \& \mathrm{w}$ are functions of x

$$
\begin{aligned}
& d(a) / d x=0 ; d(\sin u) / d x=d u(\cos u) / d x \\
& d(x) / d x=1 ; d(\cos v) / d x=-d v(\sin v) / d x
\end{aligned}
$$

$\mathrm{d}(u v w) / \mathrm{dx}=u v d w / d x+v w d u / d x+u w d v / d x+\ldots$ etc

## INTEGRALS

Note: All integrals should have a constant of integration added
Assume: $\mathrm{a}=$ fixed real $\# ; \mathrm{u}, \& \mathrm{v}$ are functions of x

$$
\begin{aligned}
& \int a d x=a x \quad \text { and } \quad \int a f(x) d x=a \int f(x) d x \\
& \int(u+v) d x=\int u d x+\int v d x ; \int e^{x} d x=e^{x}
\end{aligned}
$$

$\int(\sin a x) d x=-(\cos a x) / a ; \int(\cos a x) d x=(\sin a x) / a$


